

Signal processing and identification-AI module, Lecture 3

Classification and regression

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Classification and regression

Classification
 assigning a **class** label to the object

(Binary problem – object either belongs or does not belong to particular class)

Regression
 assigning a **value** to the object

(A continuous problem – values can be floating point numbers)

- Both are usually multidimensional
- Both are based on **features**
- Both are very similar (in terms of issues and methods used)

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Classification and regression

Training of a regressor: Minimization of a **regression error** over selected set of **training data**

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Classification and regression

Correct classification **Wrong classification**

feature 2 feature 2

feature 1 feature 1

Training of a classifier: Minimization of a **classification error** over selected set of **training data**

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Training of a classifier in general

feature 2

feature 1

Training data

Training data

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Testowanie metod

Future data

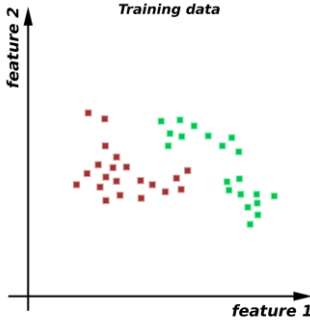
Available data

- Here we test the classifier – we estimate future accuracy
- Here we configure the classifier (i.e. select metaparameter values)
- Here we train the classifier (i.e. optimize its parameters)

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Classification and regression: clusters of data

Training data



Usually data are grouped in **clusters**

It is an advantage
(e.g. easy reduction of data amount, easier interpretation of data)

It can also be a disadvantage
(e.g. more difficult training, 'statistical' methods are more tricky to use)

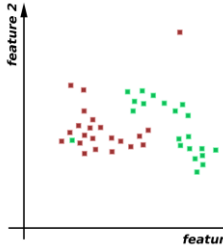
feature 2

feature 1

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Classification and regression: outliers



Single observations that are significantly different than rest of our data are called **outliers**

They are caused usually by:

- Measurement errors
- Labeling errors
- Abnormal situations in data acquisition

We usually filter them out during data acquisition and initial processing. However, sometimes it can be a bit tricky

There are ways to deal with outliers at the classification stage as well – using particular classifiers

feature 2

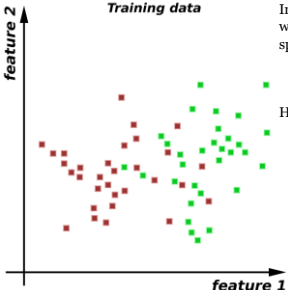
feature 1

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Overlapping of classes

Training data



In many practical situations classes overlap with each other -there exist areas in feature space occupied by more than one class

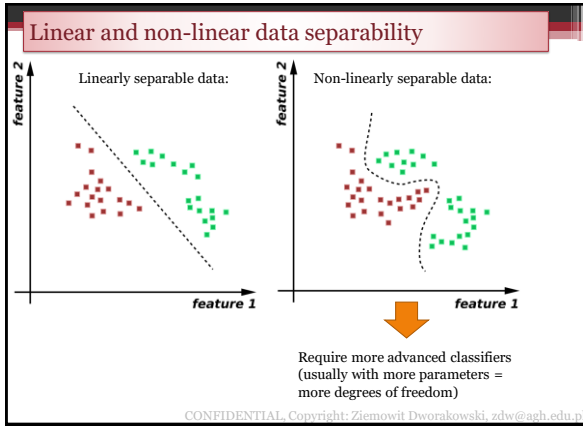
How to deal with this problem?

feature 2

feature 1

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Overfitting

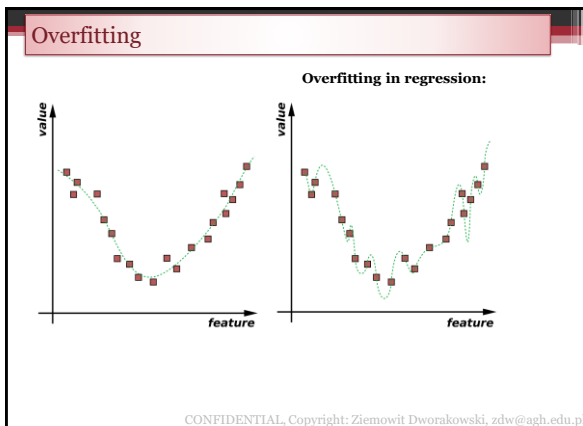
Overfitting means that classifier or regressor obtains very high accuracy on training dataset but much lower on a testing dataset

In other words:

System „memorizes” data and cannot **generalize**

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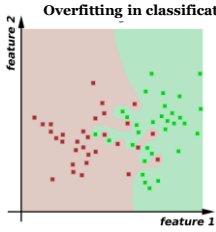
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Overfitting

Overfitting in classification:



How to avoid overfitting (How to **generalize** efficiently) ?

- A subset of data only for detecting the overfitting
- Enough training data with respect to adjustable parameters of the classifier
- Early stopping of training, regularization

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Curse of dimensionality

Level of difficulty rises exponentially with rise of problem dimensions (e.g. parameters to optimize, features to classify)

(Exponentially more data is required to fill the space reasonably well)

How to deal with the Curse of Dimensionality?

- A trivial solution: gather more data
- Pick features carefully (Only the most important)
- (in the last resort) Generate new data based on training examples

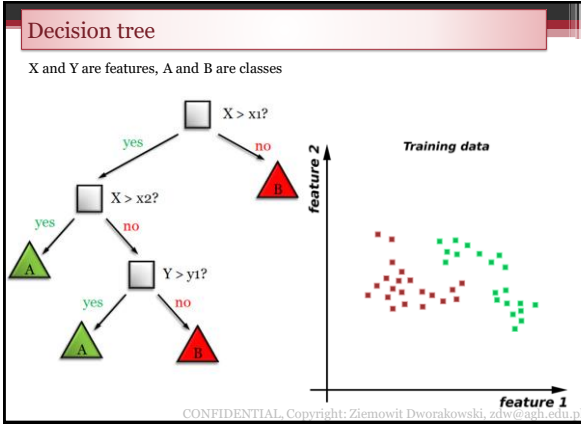
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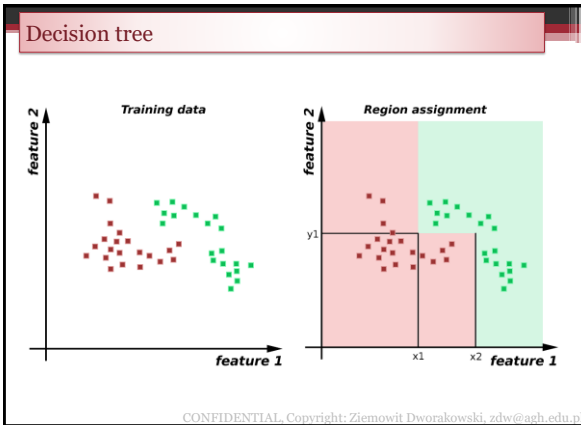
Basic classification algorithms

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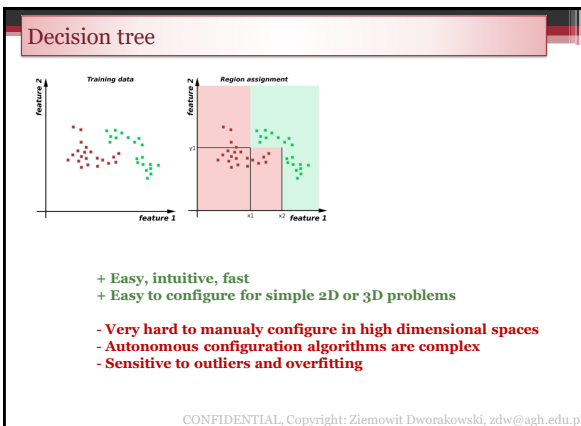
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k Nearest Neighbors, kNN

k = 1

k = 3

k = 5

In order to label a new sample:

1. Find its k (odd) closest neighbors
2. Pick a most popular label among them
3. Assign a sample with a picked label

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k Nearest Neighbors, kNN

- + Intuitive
- + Easy to implement
- + Robust to outliers (if $k > 3$)
- + Robust to overfitting

- Very sensitive to dimensionality, does not scale well
- Computationally demanding, slow, requires lots of memory

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Clustering-based classification

We know that kNN works OK but cannot handle lots of data...

We know that data are often in clusters ...

Why not use each cluster as a single data point?

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Clustering-based classification

Clustering requires assigning each sample with a **cluster label** (instead of class label) – using an **unsupervised** algorithm

After that, hopefully, we can use cluster label as class label

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Clustering-based classification

- + Saves memory
- + Efficient if data are organized in clusters
- + Intuitive
- + Robust to outliers
- + Robust to overfitting

- Hard optimization
- Detection of cluster numbers is challenging
- Works poorly for overlapping classes
- Does not allow for a complex classification margin

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Statistical – based classifiers

- + Intuitive
- + Robust to outliers
- + Robust to overfitting
- + Provide measure of probability of classification

- Sensitive to dimensionality
- Computationally and (sometimes) memory demanding – even more than kNN!

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Support Vector Machine (SVM)

- + (Very!) fast learning
- + Reasonable selection of classification margin
- + Scales well to highly dimensional feature spaces
- Requires experience in configuration
- Ignores data density

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Neural networks

- + Versatile
- + Easily scalable to higher dimensions
- + Good measure of classification certainty
- + Takes data density into account
- Requires experience in configuration
- Prone to overfitting
- non-deterministic

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Classifiers and regressors comparison

Classifier	Overall efficiency	Overfitting	Configuration	Sensitivity to dimensionality	Classification and regression?	Operational speed	Difficulty of training	Required memory
Drzewo dec.								
kNN								
Statystyczne								
Klasteryzacja								
SVM								
ANNs								
...								
...								

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Dimensionality reduction

„Curse of dimensionality“ provides a soft constraint on the number of dimensions (features). More features require much more samples.

Even if we have vast amount of data, it is usually good to reduce number of samples as much as possible as it allows usage of more (and easier) algorithms, higher efficiency, shorter computation etc.

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Dimensionality reduction

General rules:

- **Features should be significant**
(Each should contribute to the result. If discarding one of the features does not diminish the result – it was not necessary)
- **Features should be uncorrelated**
- **The number of features should be as small as possible**

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General rules

- Training, validation and testing datasets must not overlap (so we could detect overfitting both in training and in metaparameters' choice)
- If we want to artificially generate data for training, we always do it **AFTER** division of data into training, validation and testing subsets – so new data generated from one particular sample would always fall into the same subset
- Non-deterministic methods should be tested multiple times, using statistics
- We assess general accuracy, but also accuracy with respect to particular classes

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Signal processing and identification-AI module, Lecture 3

Classification and regression

- 1) Basic vocabulary: clusters of data, linear separability, outliers, overfitting, curse of dimensionality etc.
- 2) General procedure of training a classifier
- 3) Examples of classification algorithms
- 4) How to test algorithms
- 5) How to work with data

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